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Phase Diagram, Density, And Current Density Profiles Of Totally Asymmetric Simple Exclusion Process For A Junction With Two Entrances and Two Exits

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Abstract

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A dynamical model called the totally asymmetric simple exclusion process (TASEP) in one dimension (1D) is a widely-held particle hopping model which has developed into a reference model for studying non-equilibrium driven systems in particular transport phenomena. In this study, the TASEP is extended for a case of a junction with two entrances and two exits. The model is specified by a dynamical rule and boundary conditions. The dynamical rule determines the movement of particles and in this case the sequential updating dynamics is applied. The boundary condition used is the open boundary conditions, where particles may enter or exit the lattice sites. The density of the TASEP is governed by a continuity equation, which is solved numerically, such that a phase diagram a 19 the current density profiles are obtained. The result shows that there are ten density phases produced, viz.: low density, high density, coexister 12 phase, maximal current, low density-low density, high density-high density, high density-maximal current, low density-maximal current, maximal current-high density, and maximal current-low density. The current density is generally constant throughout the lattice sites, except at the junction where a spike occurs.

Keywords: current density profile, density profile, open boundary condition, phase diagram, sequential updating dynamics.

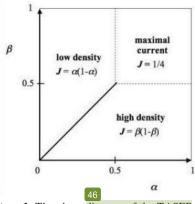
I. Introduction

The totally asymmetric simple exclusion process (TASEP) in one dimension (1D) is a standard mathematical model to investigate a wide range of non-equilibrium phenomena in physical sciences, including physics, chemistry, and biology (Chowdhury, 2003; Hinsch et.al., 2006; Shaw et.al., 2003). In general, the TASEP is a particle hopping model whereby hard core particles occupying onedimension discrete lattice sites may jump to their right nearest neighbour sites provided that there are no particles occupying the right neighbour sites. The jump may occur in one direction only, in this case, to the right. Originally, the TASEP is used to study the kinematics of polymerization (Pipkin and Gibbs, 1966; Simha and Zimmerman, 1963), e.g. for DNA and RNA synthesis on DNA templates (MacDonald et.al, 1968). Since then the model has been used to investigate one dimensional transport systems (Hinsch et.al., 2006; Chowdhury et.al., 2005; Hinsch and Frey, 2006). Variation to the TASEP has been conducted by Parmeggiani et.al. (2004) by coupling it to Langmuir kinetics. This produces a domain wall and rich phase diagram.

TASEP is a non-equilibrium driven system. A driven system is characterized by the presence of a driving force. This driving force produces currents in the system. If the current is constant but non-zero, then the system is said to be in a non-equilibrium steady state (NESS). Furthermore, the TASEP is characterized by dynamical rules and boundary conditions (Dwandaru, 2010; Dwandaru, 2006) . The dynamical rule describes the movement or jumping of particles from the sites they occupy to their nearest neighbour sites as time progresses. The dynamical rule of particles for the model on a lattice system 3 is specified systematically using an updating process on the microscopic level which is applied at each (discrete) time step. This gives the average movements or particles along 3. The dynamical rule used in this study is the sequential updating process. The updating process of this dynamical rule is that at each (discrete) time step, a site is choser 4 and omly with probability 1/(N+1), with N being the number of lattice sites. If there is a particle on the chosen site, then the particle on the chosen site may jump to its right nearest neighbour

site with rate *k* given that there is no particle occupying the right nearest neighbour site (MacDonald et.al., 1968).

The density profiles of the TASEP are described by a phase diagram. The phase diagram for the TASEP in 1D with sequential updating and open boundary conditions is based upon α on the horizontal-axis and β on the vertical-axis (shown in Picture 1). α and β may take the numerical values from 0.0 to 1.0. There are four phases of particle densities produced, viz. low density, high density, coexistence phase (along half diagonal line in Picture 1), and maximal current (Dwandaru, 2010; Dwandaru, 2006 Based on Picture 1, it can be observed that i) 1 w density (LD) occurs for $\alpha < \beta$ and α < 0.5, ii) high density (HD) occurs for $\alpha > \beta$ and β < 0.5, iii) coexistence phase (CP) occurs for α = β and α, β < 0.5, and iv) maximal current (MC) occurs for $\alpha, \beta \ge 0.5$.



Picture 1. The phase diagram of the TASEP in 1D with sequential up-dating and open boundary conditions. The horizontal axis is the constant input rate, α , and the vertical axis is the output rate, β . The equation shown is the current density of each of 3 ephase. There four phases illustrated, i.e.: low density, high density, maximal current, and coexistence phase.

Here, the objective of this research is to extend the well-known TASEP in one dimension into a less-known, but potentially important model that is the TASEP with a junction. By extending the lattice sites into a junction, the hopping of particles may be varied not just to the right nearest neighbour sites, but also to the upper neares 21 eighbour sites. Foster et.al. (1994) has studied the stationary states of a two dimensional lattice gas model with exclusion which consists of two species. Furthermore, an extensive Monte Carlo simulation has been done by Pronina

et.al. (2004) in order to study the two-channel totally asymmetric simple exclusion process. However, to the best of our knowledge, the numerical study of the TASEP for a case of a junction with two entrances and two exits has not been done before.

In this case, a special arrangement of the TASEP is put forward, i.e. joining two TASEPs in 1D at the centre of each TASEP periendicular to each other (Picture 2). Hence, the phase diagram and the current density profiles of the TASEP with a junction may be discussed based on the same respective quantities of the TASEP in 1D. For this case, the TASEP in 1D with input and output rates, α_1 and β_1 , respectively, is placed horizontally (path 1). Another TASEP in 1D with input and output rates, α_2 and β_2 , respectively, is perpendicularly joined to the first TASEP on the centre of each TASEP (path 2). In this case 432 number of lattice sites of path 1 and path 2 is taken to be the same, i.e.: N = 101. However, the joining of both paths at the centre resulted in the total number of particles of 201 lattice sites.

The jumping rates of particles are obtained upon an $N \times N$ lattice sys 5n, which is further simplified. The jum 5ng rates to the right nearest neighbour sites, i.e. from site-i to site-(i+ $\hat{\mathbf{e}}_x$), may be defined as follows:

$$k^{r} = \begin{cases} 0; & 1 \le i_{y} \le \left[\frac{[N+1]}{2} - 1\right) \\ 0.5; & i_{y} = \frac{[N+1]}{2} \\ 0; & \left(\frac{[N+1]}{2} + 1\right) \le i_{y} \le N \end{cases}$$
 (1)

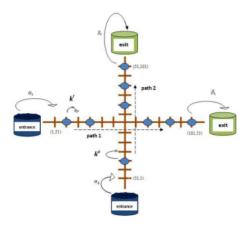
for $1 \le i_x \le N-1$,. Here, $\hat{\mathbf{e}}_x$ is the unit 5 ctor to the horizontal direction. The jumping rates to the upper arest neighbour site (along the vertical axis), i.e.: nom site-i to site- $(\mathbf{i}+\hat{\mathbf{e}}_y)$ is defined as:

$$k^{u} = \begin{cases} 0; & 1 \le i_{x} \le \left(\frac{[N+1]}{2} - 1\right) \\ 0.5; & i_{x} = \frac{[N+1]}{2} \\ 0; & \left(\frac{[N+1]}{2} + 1\right) \le i_{x} \le N \end{cases}$$
 (2)

for $1 \le i_y \le N - 1$.

For the TASEP with a junction, according to Eqs. (1) and (2) above all the jumping rates to the right $\frac{15}{(1,N+1)/2}$ to sites $\frac{(N-1,[N+1]/2)}{(N-1,[N+1]/2)}$, which is $k^r = 0.5$. Furthermore, all jumping rates to the upper nearest neighbour sites are zero, $k^u = 0.0$, except for

sites ([N+1]/2,1) to sites ([N+1]/2,N-14 which is k^{μ} = 0.5. A particle may enter site (1,[N+1]/2) or site ([N+1]/2,1) and exit site (N,[N+1]/2) or site ([N+1]/2,N) with rates α_1 , α_2 , β_1 , β_2 , respectively. Hence, the junction has two entrances and two exits.



Picture 2: TASEP in 2D for a junction with two entrances and two exits.

There are two primary physical quantities that are discussed in this research that is i) density and ii) current density. The density $[p_i(t)]$ 17 he average ensemble of particles in occupying a lattice site-i at time t. Meanwhile, the current density $[J_{i(t+1)}(t)]$ is 33 average number of hopping conducted by 42 ticles from site-i to site-(i+1) at time t. The relationship between the density and the current density is given by a continuity equation, viz.:

$$\nabla \cdot \boldsymbol{J}_{i(i+1)} = -\frac{\partial \rho_i(t)}{\partial t}.$$
 (3)

As the lattice sites are discrete, a stiple Euler method may be used to method to the left hand side of Eq. (3), that is $\nabla J_i(t) = J_{(i+1)} = 20 - J_{(i-1)i}(t)$, such that the formal solution of Eq. (3) can be written as,

$$\rho_i(t+1) = \rho_i(t) - \int_0^t dt' \left[J_{i(i+1)}(t') - J_{(i-1)i}(t') \right]. \tag{4}$$

The left hand side of Eq. (4) is obtained by modifying the right hand side of $F_{11}(3)$ considering discrete time steps, such that $\partial \rho_1(t)/\partial t = \rho_1(t+1) - \rho_2(t)$. Furthermore, the current density of the TASEP in 2D can be written as (Dwandaru, 2010):

$$J_{\mathbf{i}(\mathbf{i}+\hat{\mathbf{e}}_x)}^{r}(t) = k_{\mathbf{i}(\mathbf{i}+\hat{\mathbf{e}}_x)}^{r}(t)\rho_{\mathbf{i}}(t)[1-\rho_{(\mathbf{i}+\hat{\mathbf{e}}_x)}(t)], \tag{5}$$

nd

$$J_{\mathbf{i}(\mathbf{i}+\hat{\mathbf{e}}_{y})}^{u}(t) = k_{\mathbf{i}(\mathbf{i}+\hat{\mathbf{e}}_{y})}^{u}(t)\rho_{\mathbf{i}}(t)\left[1 - \rho_{(\mathbf{i}+\hat{\mathbf{e}}_{y})}(t)\right]$$
(6)

where Eq. (5) and Eq. (6) are the current densities of particles moving from site- \mathbf{i} to site- $(\mathbf{i}+\mathbf{\hat{e}}_x)$ and site-i to site-(i+ê_y), respectively. The equations are obtained via a relationship between the hard core lattice gas model and the TASEP extended to two dimensions (Dwandaru and Schmidt, 2001) The hard core lattice gas model is studied using density functional theory 19 FT) which is extended to lattice systems via the lattice fundamental measure theory (LFMT) (Lafuente and Cuesta, 2002; Lafuente and Cuesta, 2004). There are three relationship put forward based upon (Dwandaru, 2007), that is, (i) the particle of the TASEP is associated to the hard core particle in the lattice gas that excludes it 5 wn site, (ii) the jump of the particle of the TASEP to the right nearest neighbour site is associated to the hard core particle in the lattice gas that excludes its own and its right nearest neighbour site, and (iii) the jump of the particle of the TASEP to the upper nearest neighbour site is associated to the hard core particle in the lattice gas that excludes its own and its upper nearest neighbour site. Hence, the TASEP may be studied using the lattice gas model that consists of three species of particles. This yields three Euler-Lagrange equations of the species of particles via a variational principle. Finally, the density and current densities of the particles in the TASEP are obtained via a linearization of the aforementioned Euler-Lagrange equations.

The evolution of the density with respect to time for the TASEP in 2D may be calculated by inserting eqns. (5) and (6) into (3). This is the main partial differential equation which will be solved. The equation depends or 40 e boundary conditions specified. Hence, the input and output rates determine the density and current density profiles of the TASEP through Eqns. (5) and (6).

II. Research Method

2.1 Research Variables

Various parameters are used in this study. The parameters are described as follows: i) the input rates of particles from the reservoirs to the lattice system, that is α_1 and α_2 , and ii) the output rates of particles going out from the lattice system to the reservoirs, viz.: β_1 and β_2 , iii) the hopping rate of

particles from site-i to site-i+1 to the right near 13 neighbour, k^r , i.e.: 0.5, and iv) 11 hopping rate of particles from site-i to site-i+1 to the upper nearest neighbour site, k^u , i.e. 0.5. The independent variable utilized in this r 12 rch is the time evolution, t, of 5×10^5 time steps., and the total number of lattice sites, which is 201. Finally, the density of particles, ρ , and the current density, j, are functions of time t.

2.2 Research Design

In order to study the density and current density of the TASEP with a junction, the Dev C++ language program is applied, that is by constructing a computer code based on the parameters given above. This is done by 16 roviding a set of trial density profile into the right hand side of Eq. (4). Then calculation 49 nade on the right hand side of Eq. (4) such that a new density pr 32e is obtained. The new density profile is inserted to the right hand side of Eq. (4) and a calculation is made, such that another density profile is obtained, and so forth. This iteration procedure is terminated after the density profile corverges to its true values or the system reaches a non-equilibrium steady state. Furthermore, by varying the input and output rates, $\alpha_1 45_2$, β_1 , β_2 , respectively, the numerical values of the density and 34 rent density profiles are obtained. To observe the density and current density profiles, graphs of the density and current density as a function of the lattice sites are produced. Finally, the density phases can be determined based on the graphs and shown in a diagrammatic form.

3.1 The Phase Diagram of the TASEP in 2D for a Junction with Two Entrances and Two Exits

The four way lane TASEP in 2D with two input and two output rat 24 produces eight (8) variants of density phases, i.e.: low density (LD), high density (HD), rexistence phase (CP), maximal current (MC), low density-low density (LD-LD), high density-high density (HD-HD), high densitymaximal current (HD-MC), and low densitymaximal current (LD-MC). It may be noticed that there are four additional combinations of density phases besides the original phases obtained from the TASEP in Mary with open boundary conditions. These phases are LD-LD, HD-HD, LD-MC, and HD-MC. The aforementioned phases are obviously the result of the junction occurring in the lattice system. Table 1 is the phase diagram of the particle density of path 2 and path 1 (see Picture 2), i.e.: $\rho(\alpha_2,\beta_2)$ and $\rho(\alpha_1,\beta_1)$, respectively. The criteria for obtaining each of the density phase in Table 1 follows from the density phases of the TASEP in 1D. The LD (HD) phase is obtained if the value of the density is less (more) than 0.5 throughout the bulk. The MC phase is obtained if the value of the density is 0.5 around the bulk. Finally, the CP is gained if there is a shock (domain wall) in the density profile such that LD and HD coexist.

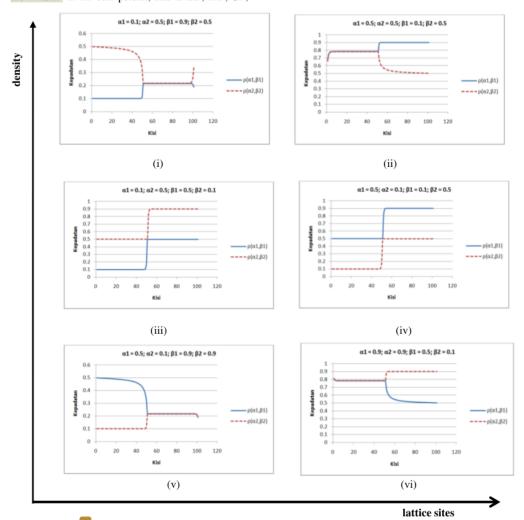
III. Results and Discussion

Table 1: The density phase diagram of path 1 and path 2, i.e.: $\rho(\alpha_1, \beta_1)$ and $\rho(\alpha_2, \beta_2)$, respectively, for the four way lane TASEP in 2D with a junction.

	<i>a</i> .2		0.1			0.5			0.9	
β_2	α_1									
		0.1	0.5	0.9	0.1	0.5	0.9	0.1	0.5	0.9
	β_1								3	
	0.1	CP	HD	HD	CP	HI	HD	CP	HD	HD
0.1	0.5	LD	MC	MC	LD-MC	HD-MC	HD-MC	LD-MC	HD-MC	HD-MC
	0.9	LD	MC	MC	LD-MC	HD-MC	HD-MC	LD-MC	HD-3C	HD-MC
	0.1	CP	MC-HD	MC-HD	CP	HD-HD	HD-HD	C ₂	HD-HD	HD-HD
0.5	0.5	LD	MC-LD	MC-LD	LD-LD	MC	MC	LD-LD	MC	MC
	0.9	LD	MC-LD	MC-LD	L 48 D	MC	MC	LD-LD	M (3)	MC
	0.1	CP	MC-HD	MC-HD	CP	HD-HD	HD-HD	CP	HD-HD	HD-HD
0.9	0.5	2 D	MC-LD	MC-LD	LD-LD	MC	MC	LD-LD	MC	MC
	0.9	LD	MC-LD	MC-LD	LD-LD	MC	MC	LD-LD	MC	MC

As mentioned before, the phase diagram of the TASEP with a junction and two input and output 10 s is similar to that of the ordinary TASEP in 1D with open boundary conditions. The main phases of the TASEP in 1D still persist, that is LD, HD, CP,

and MC. However, an additional 4 ne produces a combination of phases, which are LD-LD, HD-HD, LD-MC, and HD-MC.



Picture 3: The desity profiles of the TASEP in 2D for a junction with various input and output rates which are combinations of density profiles of the TASEP in 1D. The solid (blue) lines are the density profiles of path 1, whereas the dashed (red) line 3 are the density profile of path 2. In accordance with Table 1, profiles (i), (ii), (iii), (iv), (v), and (vi) show the LD-LD, HD-HD, LD-MC, MC-HD, MC-LD, and HD-MC phases of the density profiles of path 1, respectively.

Take for example $\alpha_2 = \beta_2 = 1.0$. Now, for the TASEP in 1D with open boundary conditions this would produce a CP where high and low densities

co-exist. However, when another lattice system is embedded in the middle and perpendicular to the previous one, then the density of the system varies with the input and output rates of the latter lattice

system. It may be observed on the upper-left corner of Table 1, as α_1 and β_1 get larger, that the phases of the system may be in LD, HD, or MC. Another case is $\alpha_2 = 0.1$ and $\beta_2 = 0.5$. Normally, for the TASEP in 1D this case produces a simple LD phase. However, the presence of the junction enriches the phases as α_1 and β_1 varies. In fact the MC-HD phase is obtained when $\alpha_1 = 0.5$, 0.9 and $\beta_1 = 0.1$. This is because many particles travel on path 1 which makes path 2 partly in MC and HD phases. However, if β_1 is increased to 0.5 or 0.9, the density phase becomes MC-LD. This is caused by the increase of β_1 , which makes the particles possibly go out from the last site of path 1, making some part of path 2 fall from HD into LD. An example of the HD phase in the TASEP in 1D is when $\alpha_2 = 0.9$ and $\beta_2 =$ 0.1. Adding another path 1 onto path 2 results in a change of the density phase. For $\alpha_1 = 0.1$ and $\beta_1 =$ 0.5 or 0.9, the phase of the system becomes LD-MC. Although there are many particles on path 2, resulted from the high α_2 and the low β_2 , the addition of path 1 makes half of the lattice sites on path 2 become LD and the rest of the lattice sites becomes MC. This means that the HD phase of path 2 may be relieved to a combination of LD and MC phase by adding another path on path 2. This is actually useful in the vehicular traffic phenomena. The last phase of the TASEP in 1D is the MC phase. As an example this is obtained when $\alpha_2 = \beta_2 = 0.9$. Adding path 2 with $\alpha_1 = \beta_1 = 0.1$ makes the system become CP. This means that adding another path lowers the density on some parts of path 2, but makes the density on the rest of the lattice sites high. Furthermore, if β_1 is increased to 0.5 or 0.9, the density of the lattice sites becomes LD-LD. This is interesting since path 2 which should be in a MC phase, because of a low density path passing through it, lowers path 2 into a LD-LD phase. Again, this might be useful in the phenomena of vehicular traffic in order to reduce congestion of traffic.

3.2 The Density Profiles of the TASEP for a Junction with Two Entrances and Two Exits

Consider some examples of the density profiles from the phase diagram give 38 n Table 1. These density profiles are graphs of the (average) density versus the lattice sites, which are obtained numerically and, in principle, are of mean-field results.

Picture 3 shows the density profiles of the TASEP in 2D for a junction with two entrances and two exits which resulted from combinations of the density profiles of the TASEP in 1D. In accordance with Table 1, the main density profiles being

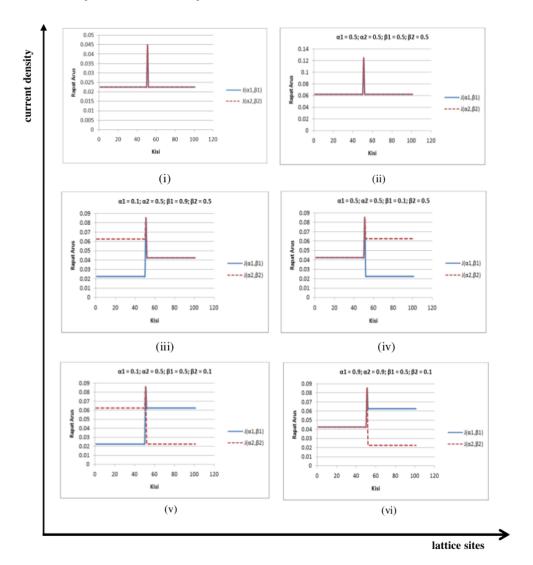
discussed are of path 1 (solid blue lines). It may be observed later that the density profiles of path 2 and path 1 are symmetrical, so that just one of the paths may be discussed. Picture 3(i) of path 1 (solid blue line) is the LD-LD phase with $\alpha_1 = 0.1$, $\alpha_2 = 0.5$, β_1 = 0.9, and β_2 = 0.5. The overall value of the density profile is lower than 0.5. However, there appears to be a small shock around the middle of the lattice site. This shock is a transition from an LD to another LD. From the beginning of the lattice sites until the middle of the lattice sites the value of the density profile is flat and constant at 0.1, but then from the middle of the lattice site until the end, the value changes suddenly to 0.2. Hence this shows coexistence between two LD phases, with coar ant values of 0.1 and 0.2, respectively. A case of the HD-HD phase is shown in Picture 3(ii) with α_1 = 0.5, $\alpha_2 = 0.5$, $\beta_1 = 0.1$, dan $\beta_2 = 0.5$. Here, the overall density profile of the solid blue line is larger than 0.5. From the beginning of the lattice sites, the profile starts from below 0.8, and then becomes flat and constant at 0.8 until the middle of the lattice site. Then an abrupt change to a flat and constant higher density of 0.9 happens until the end of the lattice site. Hence, coexistence between two high density

An example of a LD-MC phase is given in Picture 3(iii) for $\alpha_1 = 0.1$, $\alpha_2 = 0.5$, $\beta_1 = 0.5$, and β_2 = 0.1. In this case, the (solid blue line) profile starts from a flat-constant low density of 0.1 until the middle of the lattice site, and then a sudden change occurs to a flat-constant higher value of 0.5 until the end of the lattice site. Thus, coexistence between low density and maximal current occurs in this profile. Picture 3(iv) is an example of the MC-HD phase for $\alpha_1 = 0.5$, $\alpha_2 = 0.1$, $\beta_1 = 0.1$, and $\beta_2 = 0.5$. For this case, the density profile (solid blue line) is flat-constant at a value of 0.5 until at the middle of the lattice site, and then an abrupt change to a constant higher density of 0.9 until the end of the lattice site. For all cases of Picture 3(i), (ii), (iii), (iv), the coexistence occurs because of a suddent change from one phase to another. This is a characteristic of a first order phase transition which occurs because of the junction. Furtherm 36 Picture 3(v) and (vi) look similar to Picture 3(i) and (ii), where the density profiles of path 2 and path 1 are interchanged. This example shows that the density profiles 35 aths 2 and 1 are symmetric. This is also obvious from the geometric point of view of the lattice system given in Picture 2.

3.4 The Current Density Profiles of the TASEP in 2D for a Junction with Two Entrances and Two Exits

Finally, the current density profiles of the TASEP in 2D with a junction are discussed. The current density determines the average hopping of particles from one site to its nearest neighbour at each time step. As shown above, the profiles which

are being discussed are the current density profiles of path 1 (solid blue lines), i.e. *J*. These profiles are shown in Picture 4 and are in accordance with the density profiles provided in previous sections.



Picture 4: The current shitty profiles of the TASEP in 2D for a junction with two entrances and two exits. Pictu 4 (i) is the profile of the LD, HD, and CP phases. Pictures (ii), (iii), (iv), (v), and (vi) are the profiles of MC, LD-LD, HD-HD, LD-MC, and HD-MC phases, respectively.

In general it may be observed that the current density profiles are flat throughout the lattice sites, except in the middle of the lattice site where a sharp spike occurs. This sharp spike indicates that the hopping of particles at the junction is high. The constant values of the current density profiles show

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that the system reaches a non-equilibrium steady state, i.e.: a non-zero but constant current exists in the system. Hence, the applied time evolution of 5 ×10⁵ time steps is legitimate since using this time step value, the system may reach a steady state.

IV. Conclusions

From the results and discussion above, it may be concluded that the density and current density profiles of the TASEP in 2D for a junction with two entrances and two exits depend upon the input (α_1 and α_2) and output (β_1 and β_2) rates specified. The TASEP in 2D with two inputs and two 31tput rates has ten (10) density phases; namely low density (LD), high density (HD), 70 existence phase (CP), maximal current (MC), low density-low density (LD-LD), high density-high density (HD-HD), high density-maximal current (HD-MC), low densitymaximal cur 18: (LD-MC), maximal current-high density (MC-HD), and maximal current-low density (MC-LD). The first four doublety phases are equivalent to the density phases of the TASEP in 1D with open boundary conditions, whereas the other six density phases are combinations of the first four. These last six density phases are not found in the TASEP in 1D. The current density profiles are generally non-zero and constant throughout the lattice sites, except at the middle of the lattice site where a sharp peak occurs.

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